Machine Learning in Spectral CT

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To apply the CS technique in the CT field, the key is to explore the sparsity in a transform domain, and machine learning plays an important role for this goal.

2009 We developed the CS-based interior tomography theory and algorithms to solve the long-standing "interior problem" for high-fidelity local reconstruction

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Compressed sensing based interior tomography

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Abstract

While conventional wisdom is that the interior problem does not have a unique solution, by analytic continuation we recently showed that the interior problem

2012 We applied the dictionary learning technique for low-dose CT reconstruction.

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IEEE TRANSACTIONS ON MEDICAL IMAGING, VOL. 31, NO. 9, SEPTEMBER 2012

Low-Dose X-ray CT Reconstruction via Dictionary Learning

Qiong Xu, Hengyong Yu*, Senior Member, IEEE, Xuanqin Mou*, Lei Zhang, Member, IEEE, Jiang Hsieh, Senior Member, IEEE, and Ge Wang, Fellow, IEEE

Abstract—Although diagnostic medical imaging provides enormous benefits in the early detection and accuracy diagnosis of various diseases, there are growing concerns on the potential side effect of radiation induced genetic, cancerous and other diseases. How to reduce radiation dose while maintaining the diagnostic performance is a major challenge in the computed tomography (CT) field. Inspired by the compressive sensing theory, the sparse constraint in terms of total variation (TV) minimization has already better images with lower noise and more detailed structural features in our selected cases. However, there is no proof that this is true for all kinds of structures.

Index Terms—Compressive sensing (CS), computed tomography (CT), dictionary learning, low-dose CT, sparse representation, statistical iterative reconstruction.

2013 Learning based method for imaging biomarkers Funded Project (NIH/NIBIB R21 EB019074) Proposal first submission date: Nov. 2013,



IEEE TRANSACTIONS ON MEDICAL IMAGING, VOL. 36, NO. 1, JANUARY 2017



2017

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Tensor-Based Dictionary Learning for Spectral CT Reconstruction

Yanbo Zhang, *Member, IEEE*, Xuanqin Mou*, *Member, IEEE*, Ge Wang, *Fellow, IEEE*, and Hengyong Yu*, *Senior Member, IEEE*



1370

2018

IEEE TRANSACTIONS ON MEDICAL IMAGING, VOL. 37, NO. 6, JUNE 2018

Convolutional Neural Network Based Metal Artifact Reduction in X-Ray Computed Tomography

Yanbo Zhang[®], Senior Member, IEEE, and Hengyong Yu[®], Senior Member, IEEE

Original Sinogram Workflow of The **Proposed CNN-MAR Original Image** BHC Image LI Image **CNN Prior CNN Image** Forward Metal Projection Segmentation Metal Only Image Metal Trace **Original Sinogram Prior Sinogram** Forward Projection Insert Back Metal Trace Replacement **CNN-MAR Image** Corrected Sinogram FBP



UFFC

2019 EMB RESS EFF Signal Processing Society

IEEE TRANSACTIONS ON MEDICAL IMAGING, VOL. 38, NO. 4, APRIL 2019

Non-Local Low-Rank Cube-Based Tensor Factorization for Spectral CT Reconstruction

Weiwen Wu[®], Fenglin Liu[®], Yanbo Zhang[®], *Senior Member, IEEE*, Qian Wang, and Hengyong Yu[®], *Senior Member, IEEE*





Focus of this talk (Under Review)

Dictionary Learning based Image-domain Material Decomposition for spectral CT

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Material decomposition:

I. Direct material decomposition methods: directly obtain material components using x-ray spectrum from projections Pros:

- Avoid the x-ray beam hardening artifacts;
- Regularization prior can penalize material maps;

Cons:

- The real x-ray spectrum is difficult to achieved;
- Projection noise can be amplified in projection decomposition;

II. Indirect material decomposition methods: including projectionbased and image-based methods

Pros:

- The regularization prior can penalize projections or reconstructed map images;
- Image-based methods can reduce noise well;

Pros:

• Cannot avoid x-ray beam hardening artifacts;

Material decomposition methods:

Spectral CT images (attenuation maps at from all energy bins) are available using image reconstruction methods (such as FBP, etc)

- Conventional image-domain decomposition
 - Direct matrix inversion decomposition⁴

Sensitive to artifacts and noise.

- Regularized (model-based) decomposition
- Statistical measurement model + Object prior model
- Improves image quality and decomposition accuracy

Regularization methods for material decomposition:

- Material decomposition with prior knowledge aware iterative denoising (MD-PKAID)⁵
 - Retain structure details by exploring the structural redundancy
 - The material accuracy and image quality depending on prior image
- Density, local joint Sparsity and structural low-Rank (DSR)⁶
 - Artifact reduction with improvement of material accuracy
 - Ignores the physical effects with many parameters
 - Validate only on numerical phantom

[5] [Tao et al., Physical in medicine and biology, 2018]

[6] [Xie et al., Journal of Nondestructive Evaluation, 2019]





Material decomposition basic model⁷

$$\begin{bmatrix} \mathcal{G}_{11} & \cdots & \mathcal{G}_{1M} \\ \vdots & \ddots & \vdots \\ \mathcal{G}_{N1} & \cdots & \mathcal{G}_{NM} \end{bmatrix} \begin{bmatrix} \boldsymbol{f}_1 \\ \vdots \\ \boldsymbol{f}_M \end{bmatrix} = \begin{bmatrix} \overline{\boldsymbol{x}_1} \\ \vdots \\ \overline{\boldsymbol{x}_N} \end{bmatrix}$$

- ▶ $\vartheta_{nm}(1 \le n \le N, 1 \le m \le M)$ ----- averaged attenuation coefficients of the mth material at nth energy window;
- ▶ $f_m(1 \le m \le M)$ ----- m^{th} material component maps;
- ▶ $\overline{x_n}(1 \le n \le N)$ ----- spectral CT image of the n^{th} energy window.

The matrix form of Eq. (1) can be formulated as

$$\mathcal{P}_{(3)} = \mathcal{X}_{(3)}$$

$$\boldsymbol{\vartheta} = \begin{bmatrix} \vartheta_{11} & \cdots & \vartheta_{1M} \\ \vdots & \ddots & \vdots \\ \vartheta_{N1} & \cdots & \vartheta_{NM} \end{bmatrix} \in \boldsymbol{\mathcal{R}}^{N \times M}; .$$

$$\boldsymbol{\mathcal{F}} \in \boldsymbol{\mathcal{R}}^{J_1 \times J_2 \times M} \text{ and } \boldsymbol{\mathcal{X}} \in \boldsymbol{\mathcal{R}}^{J_1 \times J_2 \times N} \text{ represent two tensors;}$$

$$\boldsymbol{\mathcal{F}}_{(3)} \in \boldsymbol{\mathcal{R}}^{M \times J} \ (J = J_1 \times J_2) \text{ and } \boldsymbol{\mathcal{X}}_{(3)} \in \boldsymbol{\mathcal{R}}^{N \times J} \text{ are the mode-3 unfolding of } \boldsymbol{\mathcal{F}} \text{ and } \boldsymbol{\mathcal{X}}.$$

[7] [Wu et al., Arxiv, 2019][8] [Wu et al, IEEE Access, 2019]

(1)

(2)

Considering noise in the reconstructed images, Eq. (2) can be read as

$$\mathscr{P}_{(3)} = \mathcal{X}_{(3)} + \mathbf{\eta} \tag{3}$$

 \succ η -----the noise level

$$argmin\left(\frac{1}{2}\left\|\boldsymbol{\mathcal{X}}_{(3)}-\boldsymbol{\mathcal{G}}\boldsymbol{\mathcal{F}}_{(3)}\right\|_{F}^{2}+\lambda R(\boldsymbol{\mathcal{F}})\right)$$
(4)

R(*F*)----- the regularization term
 λ -----the regularized parameter

 $R(\mathcal{F})$ can be the Total Variation (TV), non-local mean and block matching frame and so on.

The idea of vectoried dictionary learning (DL):



Given a training set of patches, $\mathbf{x}_s \in R^{N \times 1}$, (s = 1, L, S), the dictionary learning is to solve

$$\min_{\mathbf{D},\boldsymbol{\alpha}}\sum_{s=1}^{S}\left(\left\|\mathbf{x}_{s}-\mathbf{D}\boldsymbol{\alpha}_{s}\right\|_{2}^{2}+\boldsymbol{\nu}_{s}\left\|\boldsymbol{\alpha}_{s}\right\|_{0}\right)$$

The conventional dictionary learning based image-domain material decomposition can be expressed as



- \succ F_m ----- m^{th} channel of material images \mathcal{F}
- \succ β_{*mi*} ∈ **\mathcal{R}^{T \times 1}**-----sparse representation coefficients for *i*th image patch from *m*th material image
- $\succ \quad \boldsymbol{\beta}_m = \{ \boldsymbol{\beta}_{mi} \}_{i=1}^{l}$
- > $\mathcal{H}_i(F_m)$ -----the *i*th image patch extraction operator from F_m
- \blacktriangleright **D**_m-----the trained dictionary for **m**th material
- > λ_m -----the regularized parameter for m^{th} material

Cons of conventional dictionary learning based image-domain material decomposition:

- Because a specific material map may only contain a few image features, it is difficult for the trained *D_m* to encode the image features and reduce sparse level;
- \succ training different D_m is time consuming;
- the correlation between different material maps will be lost



Three basis materials of numerical mouse

Solution

- Training a unified dictionary using image patches from all material images;
- The normalization strategy is operated on the training material image to avoid the data inconsistency of material images;

The conventional dictionary learning based image-domain material decomposition can be expressed as

$$\underset{\mathcal{F},\{\boldsymbol{\beta}_{m}\}_{m=1}^{M}}{\operatorname{argmin}} \left(\frac{1}{2} \left\| \boldsymbol{\mathcal{X}}_{(3)} - \boldsymbol{\mathcal{P}}_{(3)} \right\|_{F}^{2} + \sum_{m=1}^{M} \frac{\lambda_{m}}{2} \sum_{i=1}^{I} \left(\left\| \boldsymbol{\mathcal{H}}_{i} \left(\boldsymbol{F}_{m} \right) - \boldsymbol{D} \boldsymbol{\beta}_{mi} \right\|_{F}^{2} + v_{mi} \left\| \boldsymbol{\beta}_{mi} \right\|_{0} \right) \right)$$
(6)
The data fidelity term Dictionary learning regularization term

 \rightarrow \hat{D} -----the trained unified dictionary

Additional conditions

 If the air is also treated as one basis material, the summation of pixel values of different material images at the same location should be equal to one, i.e.,

$$\left(\sum_{m=1}^{M} \mathcal{F}_{j_1 j_2 m}\right) + AIR_{j_1 j_2} = 1 \left(1 \le j_1 \le J_1, 1 \le j_2 \le J_2\right)$$
(7)

AIR is the air map and $AIR_{j_1j_2}$ represents the binary pixel value at $(j_1, j_2)^{th}$ location. A threshold method is applied to determine the air map (0 or 1).

2 The pixel value within \mathcal{F} should be in the range of [0 1], i.e.,

$$0 \le \mathcal{F}_{j_1 j_2 m} \le 1. \tag{8}$$

Considering Eqs. (7) and (8), the proposed dictionary learning based image-domain material decomposition (DLIMD) method can be formulated as

$$\underset{\mathcal{F},\{\boldsymbol{\beta}_{m}\}_{m=1}^{M}}{\operatorname{argmin}} \left(\frac{1}{2} \left\| \boldsymbol{\mathcal{X}}_{(3)} - \boldsymbol{\mathcal{PF}}_{(3)} \right\|_{F}^{2} + \sum_{m=1}^{M} \frac{\lambda_{m}}{2} \sum_{i=1}^{I} \left(\left\| \boldsymbol{\mathcal{H}}_{i} \left(\boldsymbol{F}_{m} \right) - \boldsymbol{D} \boldsymbol{\beta}_{mi} \right\|_{F}^{2} + v_{mi} \left\| \boldsymbol{\beta}_{mi} \right\|_{0} \right) \right)$$

$$s.t. \left(\sum_{m=1}^{M} \boldsymbol{\mathcal{F}}_{j_{1}j_{2}m} \right) + \boldsymbol{AIR}_{j_{1}j_{2}} = 1, \forall j_{1}, j_{2}, 0 \leq \boldsymbol{\mathcal{F}} \leq 1.$$

$$(9)$$

Pros:

- can fully encode similarities within different material images;
- \succ can enhance the redundancy with the trained dictionary $\widehat{\mathbf{D}}$;
- save training time to some extent in practice.

Optimization

Introducing tensor u to replace \mathcal{F} , Eq. (9) can be converted into

$$\underset{\mathcal{F},\{\boldsymbol{\beta}_{m}\}_{m=1}^{M},\mathcal{U}}{\operatorname{argmin}} \left(\frac{1}{2} \left\| \boldsymbol{\mathcal{X}}_{(3)} - \boldsymbol{\mathcal{P}}_{(3)} \right\|_{F}^{2} + \sum_{m=1}^{M} \frac{\lambda_{m}}{2} \sum_{i=1}^{I} \left(\left\| \boldsymbol{\mathcal{H}}_{i} \left(\boldsymbol{U}_{m} \right) - \boldsymbol{\mathcal{D}} \boldsymbol{\beta}_{mi} \right\|_{F}^{2} + v_{mi} \left\| \boldsymbol{\beta}_{mi} \right\|_{0} \right) \right)$$
(10)
$$s.t. \left(\sum_{m=1}^{M} \boldsymbol{\mathcal{F}}_{j_{1} j_{2} m} \right) + AIR_{j_{1} j_{2}} = 1, \forall j_{1}, j_{2}, \boldsymbol{\mathcal{U}} = \boldsymbol{\mathcal{F}}, 0 \leq \boldsymbol{\mathcal{F}} \leq 1.$$

Eq. (10) can be divided into two sub-problem

$$\begin{cases} \arg \min_{\mathcal{F}} \left(\frac{1}{2} \left\| \mathcal{X}_{(3)} - \mathcal{P}\mathcal{F}_{(3)} \right\|_{F}^{2} + \frac{\eta}{2} \left\| \mathcal{F} - \mathcal{U}^{(k)} \right\|_{F}^{2} \right) \\ \text{s.t.} \left(\sum_{m=1}^{M} \mathcal{F}_{j_{1}j_{2}m} \right) + AIR_{j_{1}j_{2}} = 1, \forall j_{1}, j_{2}, 0 \leq \mathcal{F} \leq 1. \end{cases}$$

$$\arg \min_{\mathcal{U}, \left\{ \boldsymbol{\beta}_{m} \right\}_{m=1}^{M}} \left(\frac{\eta}{2} \left\| \mathcal{U} - \mathcal{F}^{(k+1)} \right\|_{F}^{2} + \sum_{m=1}^{M} \frac{\lambda_{m}}{2} \sum_{i=1}^{I} \left(\left\| \mathcal{H}_{i} \left(\mathbf{U}_{m} \right) - \hat{\mathbf{D}} \boldsymbol{\beta}_{mi} \right\|_{F}^{2} + v_{mi} \left\| \boldsymbol{\beta}_{mi} \right\|_{0} \right) \right)$$

$$(11b)$$

Optimization

As for Eq. (11a), it can be simplified as⁷

$$\underset{\mathcal{F}_{j_{1}j_{2}^{\#}}}{\operatorname{argmin}} \frac{1}{2} \left\| \left(\mathscr{G}^{\mathsf{T}} \mathscr{G} + \eta \mathbf{I} \right) \mathcal{F}_{j_{1}j_{2}^{\#}} - \left(\mathscr{G}^{\mathsf{T}} \mathscr{X}_{\# j_{1}j_{2}} + \eta \mathcal{U}_{j_{1}j_{2}^{\#}}^{(k)} \right) \right\|_{F}^{2}$$

$$\forall j_{1}, j_{2}, s.t. \left(\sum_{m=1}^{M} \mathcal{F}_{j_{1}j_{2}^{m}} \right) = 1, 0 \leq \mathcal{F}_{j_{1}j_{2}^{\#}} \leq 1.$$

$$(12)$$

Eq. (12) is a constrained least square problem and it can be easily solved.

For Eq. (11b) can be divided into the following problem

$$\underset{\mathbf{U}_{m},\mathbf{\beta}_{m}}{\operatorname{argmin}}\frac{1}{2}\left\|\mathbf{U}_{m}-\mathbf{F}_{m}^{(k+1)}\right\|_{F}^{2}+\frac{\tau_{m}}{2}\sum_{i=1}^{I}\left(\left\|\boldsymbol{\mathcal{H}}_{i}\left(\mathbf{U}_{m}\right)-\hat{\mathbf{D}}\boldsymbol{\beta}_{mi}^{(k+1)}\right\|_{F}^{2}+\nu_{mi}\left\|\boldsymbol{\beta}_{mi}\right\|_{0}\right),1\leq m\leq M \quad (13)$$

where $\tau_m = \lambda_m / \eta$, the Eq. (13) can be solved by using the method in [8]

[7] [Wu et al., Arxiv, 2019] [9] [Wu et al., APM, 2018] Outline



Implementation

- Comparisons: Direct inversion (DI) method, total variation material decomposition (TVMD) method
- The iteration number is 30 and the parameters in Table I
- The number of atoms within the dictionary are set as 512 and Image patches are 10000, patch stride 1×1
- Other parameters are in the following Table

Parameters	η	L	Patch Size	$m{arepsilon}_{ m Al/bone,Water/Tisuue,Iodine/GNP}$
Numerical mouse	3×10-5	3	10x10	(0.02, 0.057, 0.0025)
Physical phantom	0.003	10	8x8	(0.08, 0.03, 0.0025)
Preclinical experiment	0.001	12	8x8	(0.004,0.012,0.05)

Implementation

- Three indexes, i.e., RMSE, PSNR and SSIM are employed
- The unified dictionaries used in numerical mouse, physical phantom and preclinical experiment



The dictionaries are trained from DI results of numerical mouse, physical phantom and preclinical experiment [7] [Wu et al., Arxiv, 2018]

Section I: Numerical mouse

Material decomposition from FBP mouse results



The display windows of 1st-3rd columns are [0.01, 0.2], [0.25 0.55] and [0.0007 0.003]

Section I: Numerical mouse

Material decomposition from FBP mouse results



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[8] [Wu et al., APM, 2018]

Section I: Numerical mouse

Table I. Quantitative evaluation results of three basis materials.

		RMSE(10 ⁻²)	PSNR	SSIM
Bone DI TVMD DLIMD	DI	8.719	21.191	0.9314
	8.279	21.641	0.9439	
	DLIMD	7.873	22.077	0.9461
Soft tissue	DI	13.890	17.146	0.7834
	TVMD	12.910	17.782	0.8491
	DLIMD	12.368	18.154	0.8646
lodine contrast agent	DI	0.0853	61.380	0.9056
	TVMD	0.0734	62.682	0.9214
	DLIMD	0.0688	63.251	0.9393

Experiment set-up

- A micro-focus x-ray source (YXLON, 225Kv)
- A flat-panel PCD (Xcounter, XC-Hydra FX20)
- 2048 detector cells, 1080 views, 137kV, SOD: 182.68mm, SDD:440.50mm
- 256x256 image size



Setups of physical phantom experiments. (a) is the spectral CT system, (b) and (c) represent the physical phantom.

Material decomposition results



From left to right, the columns represent the decomposition results of aluminum, water and iodine, where the display windows are [0.5 1], [0.8 1] and [0 0.003].

Material decomposition results

AluminumWaterIodineTVMImage: State State

From left to right, the columns represent the decomposition results of aluminum, water and iodine, where the display windows are [0.5 1], [0.8 1] and [0 0.003].

Material decomposition results



From left to right, the columns represent the decomposition results of aluminum, water and iodine, where the display windows are [0.5 1], [0.8 1] and [0 0.003].

Table II. Quantitative evaluation results of ROI 1-5

		RMSE(10 ⁻⁴)	PSNR	SSIM
ROI-1	DI	889	21.026	0.9882
	TVMD	861	21.299	0.9882
	DLIMD	828	21.635	0.9925
ROI-2	DI	324	29.796	0.9732
	TVMD	291	30.718	0.9913
	DLIMD	271	31.329	0.9977
ROI-3	DI	5.253	65.593	0.4118
	TVMD	2.196	73.169	0.7588
	DLIMD	1.812	74.839	0.8483
ROI-4	DI	6.854	63.281	0.6200
	TVMD	3.009	70.431	0.8625
	DLIMD	2.399	72.400	0.9165
ROI-5	DI	12.530	58.041	0.6204
	TVMD	7.780	62.180	0.8549
	DLIMD	7.639	62.340	0.8945

Section III: Preclinical experiment

- PCD : PILATUS3 with 4 energy-channels by DECTRIS; It consists of 515 cells and each has a length of 0.15 mm
- Projection view is 720 and SOD = 35.27 cm, SDD = 43.58 cm
- The size of each material image is 512×512



Preclinical experiment. (a) is the preclinical specimen fixed on the spectral CT system. (b)-(e) are FBP reconstruction results from 4 energy bins, where the display window is $[0 \ 0.5] \text{ cm}^{-1}$

Section III: Preclinical experiment



The 1st-3rd rows represent the bone, soft tissue and iodine with the display windows [0.25 0.5], [0.85 0.95] and [0.0018 0.005].

Section III: Preclinical experiment

Material decomposition results



The 1st-4th rows represent the ROIs marked with "A", "B", "C" and "D", where the display windows are [0.29 0.33], [0.85 0.95], [0.85 0.95] and [0.85 0.95].

Outline



Discussion and conclusion

Discussion

- Parameters are chosen empirically in the proposed DLIMD
- The numerical mouse and two real datasets only contain three different basis materials, however the imaging objects may contain multiple (greater than 3) materials

Conclusion

- Considering the similarities of different material images, we construct a unified dictionary to encode material image sparsity by training a set of image patches
- Formulating a DLIMD mathematical model by enhancing sparsity of material maps with the dictionary
- additional constraints are incorporated into the model to further improve the decomposition accuracy



Question?

